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Citation: Low Temperature Physics **40**, 397 (2014); doi: 10.1063/1.4881175 View online: http://dx.doi.org/10.1063/1.4881175 View Table of Contents: http://scitation.aip.org/content/aip/journal/ltp/40/5?ver=pdfcov Published by the AIP Publishing

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SUPERCONDUCTIVITY, INCLUDING HIGH-TEMPERATURE SUPERCONDUCTIVITY

Low-temperature nonlinear effects in the conductivity of lightly doped cuprates $La_{2-x}Sr_xCuO_4$ in antiferromagnetic state

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Low-temperature conductivity of antiferromagnetic cuprates $La_{2-x}Sr_xCuO_4$ prepared by solid-phase synthesis was investigated. The concentration of strontium in the samples was 0.01, 0.005 and 0.001. In the temperature range T < 100 K for all the samples the conduction mechanism corresponded to 3D variable-range hopping. For $T > T_N$ (where T_N is the Neel temperature) a transition to the metallic type of conductivity was observed. Nonlinear effects in low-temperature conductivity, magnetoresistivity, as well as current-controlled negative differential resistance were found. It was established that the nonlinear behavior of conductivity intensified with decreasing the strontium concentration. For temperatures T < 10 K, the effect of positive magnetoresistance was observed. It is suggested that this effect can be attributed to the presence of a new low-temperature magnetic phase (spin density waves). © 2014 AIP Publishing LLC. [http://dx.doi.org/10.1063/1.4881175]

Introduction

Since the discovery of high-temperature superconductivity, study of cuprate superconductors (HTSC) remains one of the most important fundamental problems of solid state physics. For a long time (over 25 years), the focal point of the study of HTSC cuprates was the quest for the mechanism of high-temperature superconductivity. Despite the significant progress in this area, the exact nature of superconductivity in these compounds is still not clear. In recent years, more attention has been attracted to the cuprates in underdoped state. It is expected that their unusual properties, such as the evolution of the pseudogap state¹ or change in the dynamic coherence length of incommensurate spin fluctuations with changing the doping level,² may provide a key to understanding the nature of high-temperature superconductivity. Numerous experiments on neutron scattering and photoemission have provided detailed information on the evolution of the spin and electronic subsystems upon increasing the concentration of charge carriers in copper oxides. Nevertheless, the mechanism of metal-insulator transition in these systems remains a subject of debate. To date, it is generally accepted that the phase separation (PS),³ which is intrinsic for cuprates, creates optimal conditions for the transition from the insulating state to the normal and superconducting states. However, no consensus on the mechanism and the nature of the PS in cuprates has yet been reached. Different studies have suggested a variety of models: superconducting drops in a dielectric matrix,^{4,5} stripes,^{6,7} as well as more complex mechanisms.⁸

In order to obtain a better idea of the scenario for the transition from a Mott insulator to metallic conductivity, a

systematic study of the transport properties of cuprates in the antiferromagnetic (AFM) state with a low concentration of impurity is required. The most complete studies of weakly doped cuprates have been conducted on the $La_{2-x}Sr_xCuO_4$ system. The lowest concentration of strontium in all the cases known to us was x = 0.01. However, most of the studies of lightly doped $La_{2-x}Sr_xCuO_4$ in the dielectric state have been performed for $x \ge 0.02$, when the long-range AFM order has already been destroyed, and there are only strong AFM correlations.

In the present paper we investigated the low-temperature conductivity of ceramic samples of La_{2-x}Sr_xCuO₄ with lower strontium content: x = 0.001, 0.005, and 0.01. The aim of this work is to study the nonlinear effects in the conductivity at low temperatures. The main attention is paid to the potential impact of the structural disorder associated with the spatial distribution of strontium impurities on the low-temperature conductivity. Investigation of the mechanisms of nonlinear effects in the conductivity of the HTSC is of interest not only for solving the fundamental problems of high-temperature superconductivity, but also for a number of applications. For example, the systems in which the current-voltage characteristics (CVC) exhibit a region of negative differential resistance (NDR) are of interest for a number of technical applications. A large body of theoretical and experimental work is devoted to the quest for the conditions at which NDR can arise as well as for the systems in which these conditions can be realized. It is known that one of the conditions for NDR is the presence of impurities, defects, or inhomogeneities of any kind, which create a microscopically inhomogeneous electric field distribution inside the sample. In this regard, alloyed ceramic HTSC

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cuprates are promising materials. Due to the inherent for cuprates thermodynamic PS, these compounds have the so-called intrinsic inhomogeneities, which originate due to the intrinsic nature of a strongly correlated state of the electronic system.

The parent compound of $La_{2-x}Sr_xCuO_4$ is the stoichiometric lanthanum cuprate La_2CuO_4 , which is a hard AFM Mott-Hubbard insulator with a Neel temperature $T_N \approx 320$ K.⁹ Alloying La_2CuO_4 with an excess of oxygen or partially substituting the lanthanum atoms with divalent alkaline metals (Ca, Sr or Ba) creates charge carriers (holes) and leads to the suppression of long-range AFM order (decrease in T_N). According to the phase diagram,¹⁰ $La_{2-x}Sr_xCuO_4$ remains an insulator for x < 0.05. In the low-temperature limit ($T \rightarrow 0$), the AFM ordering persists up to the strontium concentration x = 0.02. The concentration range 0.02 < x < 0.05 is the region of strong AFM correlations.

Previously, we have investigated the conductivity of single-crystal La₂CuO_{4+ δ} in the AFM state.^{11–15} The values of T_N in these samples were in a fairly wide range of temperatures from 160 to 290 K. References 11-15 have noted the anomalies in the low-temperature behavior of conductivity, which has been interpreted as a manifestation of the competition between the localization and conductivity (or superconductivity) associated with the phase separation into the AFM phase with $\delta = 0$ and the oxygen-reach ($\delta > 0$) superconducting phase. As discussed in Ref. 11, the PS in $La_2CuO_{4+\delta}$ cuprates, most probably, does not originate from one particular mechanism. The nature of PS may depend on various circumstances, including the degree of doping. The results of our studies have demonstrated the ability to identify structural heterogeneity in HTSC based on the known phenomena of the competition between localization and superconductivity in inhomogeneous systems.^{11–15} The same kind of structural heterogeneity can be expected in lightly doped $La_{2-x}Sr_xCuO_4$ cuprates.

We assume that due to the very low concentration of strontium in addition to the general (intrinsic) heterogeneity originating from the PS, the irremovable heterogeneity associated with an external (extrinsic) factor can appear in the investigated samples of $La_{2-x}Sr_xCuO_4$. As has been shown in Ref. 16, the latter type of heterogeneity depends on the synthesis technology and is poorly controlled in the systems with low levels of doping. Conventional control methods (X-ray diffraction, electron microscopy) are not accurate enough for registering heterogeneity in such systems. On the other hand, the resistive, magnetic, and magnetoresistive properties are very sensitive to fluctuations in the distribution of an impurity. That is why these properties critically depend on such factors as temperature and time of the synthesis, annealing temperature, or the temperature rising rate. To avoid uncontrolled changes in the properties resulting from minor changes in the synthesis conditions, all the $La_{2-x}Sr_xCuO_4$ samples under study were prepared using the same technology in a single technological cycle. Due to the fact that the properties of $La_{2-x}Sr_xCuO_4$ oxides are largely determined by the synthesis conditions, and no consensus on the optimal synthesis conditions of these oxides yet exists, we will discuss the method of sample preparation here in detail.

Method of sample preparation

Samples were produced and tested at the Department of Magnetochemistry at St. Petersburg University. Ceramic $La_{2-x}Sr_xCuO_4$ samples were prepared by standard solid phase synthesis. Reagents used for production of $La_{2-x}Sr_xCuO_4$ oxides were *purissimum speciale* grade. Stoichiometric mixture of the starting reagents (lanthanum and strontium carbonate) were preliminarily calcined in air at T = 1073 K to remove the adsorbed water and carbon dioxide. The magnetic susceptibility and emission spectral analysis data confirmed the absence of ferromagnetic impurities, which could distort the measurement results, in the starting reagents. A stoichiometric mixture of the corresponding oxides and carbonates, which was calculated according the reaction equation

$$(2-x)\operatorname{La}_{2}\operatorname{O}_{3} + 2x\operatorname{SrCO}_{3} + 2\operatorname{CuO} + \frac{1}{2}\operatorname{O}_{2}$$
$$= 2\operatorname{La}_{2-x}\operatorname{Sr}_{x}\operatorname{CuO}_{4} + 2x\operatorname{CO}_{2},$$

was thoroughly grinded in an agate mortar for 1.5 h. Afterwards, the resulting mixture was cold pressed into pellets using a mold made of organic glass. The pellets were placed in a corundum crucible and calcined in air in a muffle furnace at 850 °C during 18 h. Since it has been established earlier¹⁷ that a rapid temperature rise leads to melting of the initial mixture of components (copper oxide II $(3d^9)$ decomposes into Cu₂O and O₂), the first calcination step was performed at low temperature with a gradual temperature increase of 0.5 °C/min. The synthesis temperature (850 °C) at the first stage was selected to be lower than the generally accepted value in order to ensure decomposition of strontium carbonate while reducing the risk of melting the sample. After the first stage of the synthesis, X-ray phase analysis (XRPA) was carried out using the patterns from the catalog X-Ray Diffraction Data Cards, ASTM. According to the XRPA data, in addition to the reflection lines corresponding to the standard structure of the type K₂NiF₄, two intense lines corresponding to the initial lanthanum oxide were observed in the diffractograms. This indicated that during the first step of the synthesis, complex oxides had already been formed as a result of the solid-phase reaction. However, the reaction was not completed yet. Therefore, further calcination was carried out at a higher temperature. In the second step of the synthesis, the rate of temperature increase remained the same, and the calcination temperature was set to 920 °C (4 h). Then the temperature was further raised to 950 °C (calcination time at 950 °C was 20 h) and then to 960 °C (calcination time at 960 °C was 24 h). As a result, the total calcination time in the second step of the synthesis was 48 h.

After the second stage of the synthesis, according to the XRPA data, only the reflection lines corresponding to the structure of K₂NiF₄ type were observed in the diffractograms. The unit cell parameters of the obtained structure were: a = 3.8 Å, c = 12.19 Å (for La_{1.995}Sr_{0.005}CuO₄) and a = 3.73 Å, c = 12.25 Å (for La_{1.995}Sr_{0.01}CuO₄). These values are consistent with those from the catalog Powder Diffraction Files (PDF) for the tetragonal layered structure K₂NiF₄ as well as with literature data for this structure. Thus, according to XRPA, the complex oxides obtained in this work were homogeneous and exhibited a tetragonal

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perovskite-like structure of the type K₂NiF₄. Microstructure, elemental composition of the samples, and the composition of individual phases were determined using a scanning electron microscope Cam Scan. The accuracy of determining the elemental content varied depending on the atomic number of the element and was ± 0.3 wt. % on average. A tungsten emitter at 20 keV was used as an electron source. The beam diameter was $1 \,\mu m$. The penetration depth of the radiation was 3–5 μ m. A typical micrograph of the sample La_{1.99}Sr_{0.01} CuO₄, obtained using a scanning electron microscope is shown in Fig. 1. It can be seen that the average ceramic grain size is below 1 μ m. The beam of radiation scanned the entire sample surface, followed by integral analysis. The reproducibility of the analysis results at several points on the sample indicated its high reliability. The lanthanum and copper content was determined using an EDS spectrometer LINK AN-10000. The content of strontium was determined by a highly sensitive WDS spectrometer MIKROSPEC in five different regions of the sample. Table 1 shows the results of X-ray microanalysis of three La_{2-x}Sr_xCuO₄ samples with x = 0.001, 0.005, and 0.01.

The data presented in Table 1 show that the strontium content in the sample $La_{1.99}Sr_{0.01}CuO_4$ matched the specified value (x = 0.01), while in the samples of $La_{1.999}Sr_{0.001}CuO_4$ and $La_{1.995}Sr_{0.005}CuO_4$ the strontium content in the test areas was approximately 0.002. This indicates that the spatial distribution of strontium in the samples with x = 0.005 and x = 0.001 is more inhomogeneous and the degree of structural disorder in these samples is higher than in the samples with x = 0.01.

The pellets of $La_{2-x}Sr_xCuO_4$ with the diameter of ca. 10 mm obtained in the synthesis were diced into cuboid-shaped samples using a diamond cutter. The length of the samples was 7–8 mm with the cross section of ca. 2 × 1.5 mm. These samples were used for the measurements of temperature dependence of magnetic susceptibility as well as the conductivity measurements in zero and finite magnetic fields.

Measurement results

The temperature dependence of the magnetic susceptibility $\chi(T)$ for three samples of La_{2-x}Sr_xCuO₄ was measured using a Faraday magnetometer in a magnetic field of 0.83 T.

TABLE 1. Average content of CuO, La_2O_3 , and SrO and standard deviations from the mean value (SDMV) for Sr in three samples of $La_{2-x}Sr_xCuO_4$.

Sample	CuO	La ₂ O ₃	SrO	SDMV for Sr	Total
La _{1.999} Sr _{0.001} CuO ₄	1.03	1.97	0.0020	0.0003	3.00
La1.995Sr0.005CuO4	1.01	2.00	0.0019	0.0002	3.00
La _{1.99} Sr _{0.01} CuO ₄	0.97	2.02	0.01	0	3.00

The transition temperature into the AFM state determined by the peak position on the curve $\chi(T)$ was 212, 265, and 193 K for the samples with the strontium concentration x equal 0.001, 0.005, and 0.01, respectively (Fig. 2). The dependence $\chi(T)$ shown in Fig. 2 indicates that the transition to the AFM state is smeared in temperature, hence demonstrating certain magnetic inhomogeneity of the samples. A comparison of the obtained transition temperature into the AFM state with the known phase diagram for $La_{2-x}Sr_{x}CuO_{4}$ (Ref. 10) (Fig. 3) showed that the transition to the AFM state in the La_{1.999}Sr_{0.001}CuO₄ samples occurred at a significantly lower temperature (212 K) than that expected from the phase diagram. At the same time, the magnetic state of the samples with higher strontium contents (x = 0.005 and 0.01) corresponds well to the phase diagram. In order to determine the degree of magnetic homogeneity of the samples, the magnetic susceptibility measurements were carried out on five different samples for each of the three concentrations. For all the concentrations, a small spread in T_N was observed, which was $\pm 7\%$ (for x = 0.001 and 0.01) and $\pm 4\%$ (for x = 0.005). Substantial deviation of the T_N values downwards from the AFM transition line on the phase diagram was found only for the samples with a minimum content of strontium x = 0.001. The deviation was about 90 K and could not be associated with the magnetic inhomogeneity of the samples, which was recorded by the magnetic measurements.

Using the obtained values of Neel temperature and the data from Ref. 18, we can estimate the average number of holes per copper atom. For samples with x = 0.001 and 0.01 it was 0.00552 and 0.00654, respectively (Table II). It seems surprising that upon a ten-fold decrease in the concentration of strontium in the furnace charge, the value of T_N and the



FIG. 1. Micrograph of a $La_{1.99}Sr_{0.01}CuO_4$ ceramic sample obtained using a scanning electron microscope.



FIG. 2. Temperature dependence of the magnetic susceptibility for three $La_{2-x}Sr_xCuO_4$ samples in a magnetic field of 0.83 T.

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FIG. 3. Dependence of the Neel temperature T_N on strontium concentration. The dotted line corresponds to the position of the AFM phase-transition line in the phase diagram.¹⁰ Points correspond to the experimental values of T_N obtained in this work for four samples of La_{2-x}Sr_xCuO₄.

hole concentration in the sample with x = 0.001 were just slightly changed as compared to the sample with x = 0.01. The Neel temperature has increased by 10%, and the hole concentration decreased by about 16%. These data indicate that there are localized regions in the La_{1,999}Sr_{0,001}CuO₄ samples, in which the concentration of strontium may be substantially higher than not only 0.001, but also 0.002 measured by X-ray microanalysis (Table 1) in the test parts of the sample. Thus, the results of X-ray microanalysis and magnetic measurements show that the decrease in strontium concentration is accompanied by an increase in the degree of structural disorder associated with non-unifrom bulk distribution of strontium. Among the all investigated samples, the samples with a minimum content of strontium (x = 0.001) were found to be the most heterogeneous. Manifestation of structural disorder should also be expected in the behavior of the low-temperature conductivity.

For resistance measurements, four samples with known values of T_N and various degrees of doping strontium were used. The resistance measurements were carried out in fourprobe geometry in the current-driven regime. Contacts to the samples were made using silver paste. The data on the temperature dependence of the resistivity for three samples with different content of Sr, which were obtained at a current $J = 100 \ \mu$ A, are shown in Fig. 4. At temperatures below 100 K, all the samples obeyed the Mott law for 3D variablerange hopping conductivity:¹⁹ $R(T) \propto \exp[(T_0/T)^{1/4}]$. Upon decreasing temperature, there was a marked deviation from the Mott law towards a lower resistance. For a fixed current of 100 μ A, as the concentration of strontium decreased, the

TABLE 2. Neel temperature T_N , the concentration of holes per unit cell, the characteristic temperature T_0 , and the localization length L_c for La_{2-x}Sr_xCuO₄ samples with different concentrations of Sr.

Sample	<i>T_N</i> , K	<i>n</i> /atom Cu	$T_0, 10^6 { m K}$	L_c , nm
La1.999Sr0.001CuO4	212	0.00552	1.25	0.32
La _{1.999} Sr _{0.001} CuO ₄	201	0.00608	1.757	0.287
La1.995Sr0.005CuO4	265	0.00257	1.996	0.275
$La_{1.99}Sr_{0.01}CuO_4$	193	0.00654	0.36	0.478



FIG. 4. Temperature dependence of the resistivity for three samples of $La_{2-x}Sr_xCuO_4$.

temperature at which deviation from the Mott law begins was observed to shift toward higher temperatures, and the temperature range of validity of the Mott law narrowed. For $T > T_N$, a transition to the metallic conductivity was observed in all the samples. This transition is consistent with the well-known theoretical concepts and some experiments.²⁰ According to these concepts, the AFM order enhances the localization of holes, while thermal excitation destroys the AFM order and causes the delocalization of carriers. Therefore, above T_N the system may approach the metallic state upon increasing temperature.

Using the experimental values of T_0 and the theoretical expression $kT_0 \approx 16/[N(E_F)L_c^3]$, ^{19,21} it is possible to estimate the localization length L_c from the charge-carrier density of states in La₂CuO₄ at the Fermi level $N(E_F) = 2.8 \times 10^{46} \text{ J}^{-1} \text{ m}^{-3}$.²² Table 2 shows the Neel temperatures, hole concentration, and average localization length L_c , which were calculated using the data of resistivity measurements at a current $J = 100 \ \mu\text{A}$ (Fig. 4). For all the samples, the average length of localization was comparable with the lattice parameters in the plane CuO₂.

It should be noted that despite the close values of charge-carrier density in the samples with x = 0.01 and 0.001 obtained from the magnetic measurements, the localization length L_c was considerably different in these samples: L_c in the La_{1.999}Sr_{0.001}CuO₄ samples was substantially smaller than that in La_{1.999}Sr_{0.001}CuO₄ and La_{1.995}Sr_{0.005}CuO₄ exhibited similar values of L_c (Table 2) as well as similar values of $\rho(T)$ at low temperatures (T < 100 K) (Fig. 4). In other

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words, the La_{1.999}Sr_{0.001}CuO₄ and La_{1.995}Sr_{0.005}CuO₄ samples exhibited similar electrical properties. However, unlike $La_{1.995}Sr_{0.005}CuO_4$, the sample of $La_{1.999}Sr_{0.001}CuO_4$ showed no correlation between the magnetic (the values of T_N and n) and electrical (L_c) measurements. This discrepancy may be due to the fact that the applied expression for $T_N(n)$ was obtained in Ref. 18 for the case of very homogeneous samples. Since the sample La_{1,999}Sr_{0.001}CuO₄ exhibits strong structural disorder, it is not correct to apply the dependence $T_N(n)$ from Ref. 18 for the estimation of charge-carriers density in this sample. Thus, the above discrepancy between the results of resistive and magnetic measurements supports the assumption of a higher degree of inhomogeneity (and thus structural disorder) in the ceramics with x = 0.001. The mechanism of such a strong suppression of the AFM order that we observe in the samples La_{1,999}Sr_{0,001}CuO₄ is not clear and requires further study.

The assumed spatial heterogeneity of the distribution of Sr impurity arises on the nanoscale level, comparable to the localization length. Since the beam diameter and the penetration depth of radiation in the electron-microscopy measurements are of several orders of magnitude larger than the characteristic scale of inhomogeneities, the inhomogeneous distribution of strontium cannot be detected by scanning electron microscopy.

In the case of very small calculated average localization length and low carrier concentration, the conductivity should be percolative in nature. In such a case, the maximum anomalies in the behavior of $\rho(T)$ should be expected at low temperatures, when a limited number of current channels determine the total conductivity of the system.

In the region $T < T_N$, the behavior of ρ (T) strongly depends on the current (Figs. 5 and 6). It can be seen that increasing the transport current leads to the reduction of the region of validity of the Mott law and an increase in nonlinear effects in conductivity. Moreover, the increase in current is accompanied by a slight decrease in the slope of the curves $\rho(T^{-1/4})$ in the region where the Mott law is obeyed and a corresponding increase in the localization length (Fig. 7). When the current is reduced, the temperature of the onset of deviation of $\rho(T)$ from the Mott law decreases. The $\rho(T)$ data for the sample La_{1.999}Sr_{0.001}CuO₄ ($T_N = 201 \text{ K}$) (Fig. 6) show that for measuring current of 0.03 μ A, the Mott law holds down to 5 K. We believe that the minimum critical current at which the Mott law is obeyed down to helium temperatures depends on the concentration of charge carriers and the quality of the sample (degree of structural disorder). The low-temperature behavior of $\rho(T)$ shown in Figs. 5 and 6 corresponds to that of percolative conductivity. Regardless of the nature of structural disorder in heterogeneous granular systems, the conductivity is determined by the optimal chains of grains with the maximum probability of tunneling between the adjacent grains separated by intergranular barriers. In the case of thermally activated conductivity, the number of conducting chains gradually decreases with decreasing temperature and, at a sufficiently low temperature, the percolation network can be reduced to a single conducting channel. These optimum chains have several high-resistance tunnel junctions with high activation energy, which determine the thermally activated character of the measured total conductivity. At a fixed temperature the



FIG. 5. Temperature dependence of the resistivity for two samples: $La_{2-x}Sr_xCuO_4$ with $T_N = 212 \text{ K}$ (x = 0.001) and $T_N = 193 \text{ K}$ (x = 0.01) for various values of the transport current. Arrows indicate transition to the metallic type of conductivity.

spatial distribution of the optimal chains and the position of high-resistance contacts, which determine the system impedance, constantly change with external electric field (current). Furthermore, upon increasing the external field, additional transport channels appear. In this scenario, $\rho(T)$ in Fig. 6 first



FIG. 6. Temperature dependences of resistivity for the La_{1.999}Sr_{0.001}CuO₄ sample with $T_N = 201$ K for different values of transport currents.



FIG. 7. Dependence of the charge-carrier localization length L_c on the current for two samples of La_{2-x}Sr_xCuO₄.

drops rather sharply when the current increases from 0.03 to 0.2 μ A. This corresponds to an increase in the number of conducting channels with increasing current. With a further current increase in the range of 0.2–2 μ A, the resistance barely changes, which corresponds to Ohm's law. At a current $J > 2 \mu$ A the resistance decreases with increasing current.

Thus, in the case of structural inhomogeneity of the samples, the behavior of $\rho(T)$ exhibits current- and temperaturecontrolled nonlinear effects in conductivity.

To elucidate the possible mechanisms of the nonlinear behavior in conductivity we need to consider in detail the non-ohmic effects in current-voltage characteristics. For the La_{1.999}Sr_{0.001}CuO₄ ceramics both current-voltage and magnetoresistance (MR) measurements were carried out on one sample with $T_N = 212$ K.

Fig. 8 shows the current-voltage characteristics measured at 4.4 K on three samples with different concentrations of strontium and plotted on a logarithmic scale. It can be seen that an increase in current is accompanied by a nonmonotonic change in voltage. The currents J_{c1} and J_{c2} in Fig. 8 correspond to the condition dU/dJ = 0, i.e., the derivative dU/dJ changes sign at the points J_{c1} and J_{c2} . Above a certain threshold current J_{c1} , a switch into the NDR regime occurs (dU/dJ < 0). With a further current increase (J > 0) J_{c2}), the derivative changes its sign again: dU/dJ > 0. The experimental data on U(J) obtained from the measurements of $\rho(T, J)$ (Fig. 5) matched the directly measured CVC with a fairly good accuracy. This confirms validity of the conducted measurements. Straight lines in Fig. 8 correspond to the dependence U(J) which is close to linear. Significant deviations from the linear dependence U(J) were observed both at low and at high currents. At low currents (J < 2 $\times 10^{-6}$ A for x = 0.01), the behavior of U(J) at 4.4 K corresponds to the resistance decreasing with increasing current.



FIG. 8. Dependences U(J) for three samples of La_{2-x}Sr_xCuO₄ at 4.4 K. The inset shows the dependence of the transition current to the NDR regime J_{c1} on the concentration of strontium.

Nonlinear behavior of this type is determined by the tunneling of carriers between isolated conductive chains near the percolation threshold, when a continuous conducting cluster has not yet formed.²³ In this regime, an increase in electric field (and the corresponding increase in current) leads to a higher tunneling probability (or higher jumping probability) and an increase in conductivity. With a further increase in current, a transition to a close-to-ohmic regime takes place. At low temperatures ($T \le 10$ K), a nearly linear dependence of U(J) was observed in a very narrow range of low currents. For the more homogeneous sample La_{1.999}Sr_{0.01}CuO₄ at 4.4 K, this interval was approximately 2–40 μ A (Fig. 8).

In all investigated samples, the NDR regime was only observed at low temperatures. The transition temperature to the NDR regime increased with decreasing the concentration of strontium. According to the dependences shown in Figs. 9 and 10, for the more homogeneous sample with x = 0.01 the NDR regime is observed for $T \le 10$ K. For less homogeneous samples, the transition to the NDR regime occurs at higher temperatures: 20 K for x = 0.005 and 30 K for x = 0.001. At a fixed temperature, the current J_{c1} , at which the transition to the NDR regime occurs, depends on the concentration of strontium and decreases with decreasing the concentrations x = 0.005 and 0.001, the currents J_{c1} are similar and roughly an order of magnitude smaller than the current of NDR transition for the sample with x = 0.01.

Therefore, an increase in structural disorder upon decreasing the concentrations of strontium leads to a reduction in the threshold current J_{c1} and increase in the threshold temperature for the transition to the NDR regime. For a given concentration of strontium, the current J_{c1} increases with temperature (Figs. 9 and 10).

We evaluated the effect of electric field on conductivity in the regime of variable-range hopping¹⁹

$$R(T,E) = R_0(T)\exp(-eEr_h\gamma/kT),$$

where $R_0(T)$ is the resistance at $E \rightarrow 0$, r_h is the average length of a jump, and γ is a numerical factor of the order of unity. It follows from this expression that at sufficiently low fields when $eEr_h\gamma/kT \ll 1$, the resistance does not depend on the field. Estimates have shown that this inequality holds for



FIG. 9. Current-voltage characteristics for three $La_{2-x}Sr_xCuO_4$ samples at different temperatures *T*, K: 4.4 (\Box), 5 (\blacksquare), 10 (\bigcirc), 20 (\bullet), 30 (\triangle), and 50 (\blacktriangle).

the studied samples even at the highest fields we could achieve. Thus, the observed nonlinear behavior of CVC and the presence of the NDR region (Figs. 9 and 10) cannot be explicitly linked to the influence of the average electric field.



FIG. 10. Temperature dependences of the transition current to the NDR regime J_{c1} for three samples of La_{2-x}Sr_xCuO₄.

It should be noted that for the investigated samples of $La_{2-x}Sr_xCuO_4$ the transition to the NDR regime occurs in a relatively low field, when the field strength in the sample reaches $E_c \sim (5-10)$ V/cm. In conventional semiconductors the NDR region begins at significantly higher threshold fields. (For example, estimates for the threshold field in GaAs give value $E_c \sim 3000$ V/cm.²⁴) With increasing temperature, the threshold field E_c in $La_{2-x}Sr_xCuO_4$ decreases (Fig. 9), whereas the threshold current J_{c1} increases (Fig. 10).

Therefore, we found that increasing the degree of structural disorder upon decreasing the concentrations of strontium leads to an increase in the non-linear effects in the conductivity of $La_{2-x}Sr_{x}CuO_{4}$ ceramic samples. Compositional heterogeneity of the samples leads to an inhomogeneous spatial distribution of charge carriers, which creates a non-uniform electric field distribution inside the sample. This may result in the appearance of regions where the local electric field substantially exceeds the average value (5-10) V/cm. In such regions a local overheating of the charge carriers can occur. The temperature of the charge-carriers then becomes higher than the temperature of the phonons if the carriers are not able to transfer the energy acquired from the field to the crystal lattice fast enough. The heating of the charge carriers leads to a change in mobility hence resulting in a violation of Ohm's law.

Spatial inhomogeneity of the field distribution is always greater in the samples with a higher degree of structural disorder, so the overheating of electrons is also stronger there. As a result, the transition to the NDR regime in these samples may occur at lower currents and higher temperatures, as was observed in our experiments.

The behavior of magnetoresistance (MR) in the investigated La_{2-x}Sr_xCuO₄ samples also exhibits a strong dependence on the transport current (Fig. 11). The MR is positive for $T \leq 10$ K at relatively low currents. When the temperature and (or) current increases, the positive MR decreases and becomes negative (Figs. 12 and 13). The positive MR is higher for the sample with a higher concentration of Sr (x = 0.01). For example, in a field of 1.3 T at T = 4.4 K and current $J = 1 \ \mu A$, the positive MR was 9.5% (x = 0.01) and 1.6% (x = 0.001). The same ratio was demonstrated by the dependence of the MR on the current at T = 7 K (Fig. 13). For all the values of measurement current the positive MR was higher for the less resistive sample with x = 0.01. The current at which the transition to the negative MR occurs is significantly higher for the sample with x = 0.01 (Figs. 11 and 13).

Discussion

It is of interest to compare the results obtained in this paper with earlier studies of nonlinear effects in conductivity of single-crystal La₂CuO_{4+ δ}. For instance, in Refs. 14 and 15 the features of the low-temperature behavior of $\rho(T)$ in the two investigated La₂CuO_{4+ δ} single crystals have been explained by the presence of superconducting inclusions¹⁵ or isolated superconducting chains in a dielectric matrix.¹⁴ In the both La₂CuO_{4+ δ} single-crystals the behavior of $\rho(T)$ and U(T, J) at low temperatures was nonlinear. Upon increasing

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FIG. 11. Magnetic-field dependence of the magnetoresistance for two samples of $La_{2-x}Sr_xCuO_4$ at T = 4.4 K and different values of transport current **J** || **H**.

the current to a certain temperature-dependent critical value J_c , the transition to the NDR regime occurred.

To explain the experimentally observed deviations from Ohm's law in doped semiconductors, the theory of "hot" electrons is often engaged.²⁵ For example, in Ref. 26 for doped Ge in the regime of hopping conductivity, a satisfactory quantitative description of the nonlinear behavior of experimental CVCs has been obtained. The calculation has been performed with the electron overheating and the "thermal model" of the energy transfer from the electron to phonon subsystem taken into account. It has been assumed that the resistance of the sample depends only on the electron temperature T_e whatever current is applied. In the case



FIG. 12. Magnetic-field dependence of the magnetoresistance for a sample of La_{1.99}Sr_{0.01}CuO₄ at different temperatures and $J = 10 \ \mu$ A.



FIG. 13. Current dependence of the magnetoresistance for samples of $La_{2-x}Sr_xCuO_4$ with different values of x: 0.01 (\bigcirc) and 0.001 (\bigcirc). T = 7 K; H = 1.5 T.

discussed in Ref. 26, the nonlinear CVCs are due to the fact that the sample resistance $R(T_e)$ decreases upon heating the charge carriers to T_e . As a result, the voltage on the sample $U=JR(T_e)$ may decrease with increasing the current. Below a certain critical temperature T_x , an extremal point dU/dJ = 0appears on the CVCs, followed by an NDR region. The NDR region is an area of instability, current and resistance oscillations, and non-equilibrium transitions. As has been shown in well-known theoretical studies, one of the possible causes of NDR is inhomogeneous distribution of impurities and defects, which creates regions with a different strength of electric field in the crystal.²⁵

In single-crystal La₂CuO_{4+ δ} samples with Neel temperature $T_N = 182 \text{ K}$ (Ref. 14) and 269 K,¹⁵ superconducting inclusions in a dielectric matrix have been considered as the inhomogeneities responsible for the emergence of NDR. It was found that the qualitative shape of the CVCs for $La_2CuO_{4+\delta}$ matches the dependences calculated with the electron overheating taken into account in Ref. 26. The critical temperature of the transition to NDR regime in Ref. 14 was approximately (5-6) K. The estimates based on the thermal model²⁷ have resulted in a value close to 1 K. However, this discrepancy may be due to the phase separation into superconducting and insulating regions. The model of Refs. 26 and 27 has been developed for semiconductors and hence does not comprise superconducting inclusions acting as inhomogeneities. Nevertheless, the main conclusions of the model^{26,27} are consistent with the experimental results obtained in Refs. 14 and 15.

The MR behavior in the temperature range 5-30 K and current range $0.1-100 \ \mu\text{A}$ (Ref. 14) correlates with the behavior of R(T, J) and CVCs and corresponds to the presence of sufficiently long superconducting chains in a

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dielectric matrix. At low temperatures ($T \le 8$ K) and relatively low currents, the positive magnetoresistance associated with the suppression of superconductivity by a magnetic field has been observed in Ref. 14. Upon increasing the current to $J \ge 10 \ \mu$ A there was a transition from positive to negative MR.

In the single crystal La₂CuO_{4+ δ} with $T_N = 269$ K (Ref. 15) no correlation between the behavior of R(T,J) and MR has been observed. In Ref. 15 a transition from the Mott law to simple thermally-activated conductivity R(T) $\propto \exp{(\Delta/kT)}$, where $\Delta = 32.4$ K and k is the Boltzmann constant, has been observed at T < 25 K and $J \le 0.2 \mu$ A. As has been shown in Ref. 11, such a transition at low temperatures indicates the formation of isolated superconducting inclusions in a dielectric matrix. In this case the suppression of local superconductivity by magnetic field should lead to the unpairing of charge carriers and a resistance decrease. However, in Ref. 15 only positive MR has been observed in this range of temperatures and currents. To explain the positive MR, Ref. 15 has used the hypothesis²⁸ on the formation of a new low-temperature magnetic phase coexisting with the superconducting phase. As has been shown by the studies of phase separation in the lanthanum cuprate samples with excess of oxygen, the dielectric phase in the mixed state below 40 K is not a Neel phase but represents a new magnetic state-spin density waves (SDW).²⁸ The relative amount of this phase increases with decreasing the excess of oxygen (and the corresponding decrease in T_c). Therefore, the content of the magnetic phase is higher in a weakly doped $La_2CuO_{4+\delta}$ and, respectively, the content of the superconducting phase is lower. Magnetic field stabilizes the magnetic phase by reducing the volume fraction of the superconducting phase, hence mimicking changes in the doping level.²⁸ Such collective excitations as SDW carry thermal energy and, when propagating, scatter on each other, phonons, impurities and crystal boundaries. At the same time they serve as scattering centers for other quasiparticles, including electrons and holes. Scattering of charge carriers by spin excitations gives an additional contribution to the resistivity. Thus, since magnetic field stabilizes the magnetic phase, it should also induce positive MR. In the vicinity of a defect (e.g., strontium or oxygen atom), there is an additional spin density redistribution. As a result, positive MR may depend on the concentration and distribution of impurities in the crystal.

In the present study of $La_{2-x}Sr_xCuO_4$ ceramic samples, the $\rho(T)$ dependences are fundamentally different those observed previously in single-crystalline $La_2CuO_{4+\delta}$.^{14,15} At low temperatures, these dependences cannot be explained by the presence of superconducting inclusions at currents $J \ge 0.5 \ \mu\text{A}$ (Figs. 4 and 5) and even $J \ge 0.03 \ \mu\text{A}$ (Fig. 6). This is surprising since the parameters determining the conductivity and the temperature dependence of resistivity (hole concentration *n* and the carrier localization length L_c) in the studied $La_{2-x}Sr_xCuO_4$ ceramic samples and $La_2CuO_{4+\delta}$ single crystals are similar.^{14,15} For example, for La₂CuO_{4+ δ} (Ref. 15) n = 0.0024 and $L_c \cong 0.262$ nm, while for $La_{1.995}Sr_{0.005}CuO_4 n = 0.00257$ and $L_c \cong 0.275$ nm (Table 2. And, for the $La_{1.999}Sr_{0.001}CuO_4$ sample the estimated value of hole concentration and the average localization length were even higher than those for the single crystal La₂CuO_{4+ δ} studied in Ref. 15. The $\rho(T)$ dependence for

 $La_{2-x}Sr_xCuO_4$ was qualitatively different from those for $La_2CuO_{4+\delta}$ (Refs. 14 and 15) also at high temperatures. For $T > T_N$, all the La_{2-x}Sr_xCuO₄ samples exhibited the transition to the metallic type of the $\rho(T)$ dependence (Figs. 4–6), whereas in La₂CuO_{4+ δ}^{14,15} the insulator-metal transition has not been observed. Thus, the comparison of experimental data on conductivity for two closely related systems, $La_{2-x}Sr_{x}CuO_{4}$ and $La_{2}CuO_{4+\delta}$, shows that the features of the transport properties of cuprates in the AFM state are determined not only by the density of charge carriers and their degree of localization. We believe that various kinds of correlation effects related to the nature of structural disorder have a significant impact on conductivity as well. A particular role can be played by the so-called non-universal disorder, i.e., strongly correlated structural fluctuations. Examples of the non-universal disorder are the precipitates of another phase, accumulation of impurities inherent to HTSC cuprates, and orientational disorder occurring at the grain boundaries in ceramics. In single crystals, dislocations and (or) twin boundaries are additional sources of the non-universal structural disorder. In addition, structural differences between $La_{2-x}Sr_{x}CuO_{4}$ and $La_{2}CuO_{4+\delta}$ arise due to the fact that the excess oxygen and strontium atoms occupy different positions in the lattice of La_2CuO_4 . At the same time, the disturbances produced by the excess oxygen and strontium atoms in the lattice of La₂CuO₄ have significant differences. These perturbations depend both on the structure factor (position of the impurity in the lattice of the matrix) and the form factor of the impurity potential. Since strontium is a substitutional element, its atoms should produce a stronger perturbation in the periodic lattice potential than oxygen, similar to the case of substitutional impurities in the metals. For example, it has been noted in Ref. 29 that the substitution of La by Sr leads to the interaction potential Sr-O in the direction perpendicular to the CuO₂ layers of about 25 eV. This is 30 times higher than the interaction potential La–O and 100 times higher than that in Cu-O. Molecular dynamics calculations have shown that as a result of substitution of La atoms by Sr, there occurs an excitation of local high-frequency oscillations (LHFO) of four oxygen atoms in the CuO₂ layer in the vicinity of Sr atoms with an energy of about 0.4 eV.^{29,30} Some fraction of the thermal oscillation energy is localized in small areas due to "capture" of the LHFO by defects. In the vicinity of Sr atoms "hot spots" appear, while the rest of the system is efficiently cooled. The degree of localization of the energy of thermal oscillations depends on the concentration of "defects," i.e., the concentration of Sr. In this case the characteristic size of the "hot spots" can reach 10 A. Similar calculations performed under the assumption that the impurities are uniformly distributed throughout the crystal have not shown the excitation of LHFO. In summary, the calculations^{29,30} have shown that the lattice dynamics and transport properties of HTSC are affected not only by the type of impurity and its concentration, but also by the particular nature of structural disorder.

The fact that the low-temperature behavior of $\rho(T)$ in the La_{2-x}Sr_xCuO₄ samples with strontium content $x \leq 0.01$ cannot be explained by the presence of superconducting inclusions, can be attributed to a very small size of the precipitates of the phase with a high content of strontium. It is known that the properties of a superconducting grain

significantly change when its size is reduced to a few nanometers. Superconductivity might not be observed if the distance between the size-quantization levels in a grain exceeds the superconducting gap Δ of the bulk material.³¹ Another scenario for suppression of superconductivity in $La_{2-x}Sr_{x}CuO_{4}$ is related with the possible formation of "hot spots."29 At sufficiently low concentrations of strontium, the size of the region rich in strontium (and in charge carriers) can be comparable with the size of the "hot spots." Superconducting pairs are not formed in the "hot" region due to the heating of carriers, while the "cold" region is depleted of charge carriers. It is also possible that in the case of extremely low concentration of Sr (x < 0.01) there is no macroscopic PS. It is known that the PS occurs only for a sufficiently high degree of doping. Due to the high mobility of excess oxygen atoms in the $La_{2-x}Sr_xCuO_4$ cuprate, which is due to the oxygen segregation on various structural and interphase boundaries, in samples with low oxygen content the aggregations of the embedded oxygen atoms near the boundaries can favour PS in a limited region of space. In lanthanum-strontium cuprate, the strontium ions are practically immobile, so impurity or thermodynamic phase separation may not occur.

Regardless of the mechanism of the suppression of local superconductivity in $La_{2-x}Sr_xCuO_4$, the current-controlled NDR effect observed in the present paper can be attributed to a known type of NDR in percolation systems,³² in which an increase in the electric field (current) leads to the elongation of the existing or even the formation of new non-continuous percolation paths with high conductivity. A further current increase under the condition of strong heterogeneity may lead to the local heating of charge carriers and an increase in their mobility. Both of these mechanisms lead to a decrease in the electrical resistance. The extent of heating will be stronger, the higher is the degree of structural disorder, so the current at which the transition to NDR regime occurs decreases with decreasing the concentration of strontium.

Since the emergence of local superconductivity in $La_{2-x}Sr_xCuO_4$ samples with $x \le 0.01$ seems unlikely, we believe that, as in the case of $La_2CuO_{4+\delta}$,¹⁵ the mechanism of positive MR in the AFM samples of La_{2-x}Sr_xCuO₄ may be related with the formation of SDW.²⁸ For all the investigated samples of $La_{2-x}Sr_xCuO_4$, the positive MR occurred only at sufficiently low temperatures ($T \le 10 \,\mathrm{K}$) with the currents $J < J_c$. With increasing temperature or current, thermal fluctuations and the local heating of charge carriers destroy spin ordering. This leads to a decrease in the number of scattering centers (SDWs act as scattering centers too) for charge carriers and the resistance decreases. The same effect is also caused by structural fluctuations. Therefore, in less homogeneous samples with lower strontium content, the positive MR is lower and disappears for lower values of the current (Figs. 11 and 13) and (or) temperature. Upon the complete suppression of SDW, the magnetoresistance becomes negative.

This mechanism for the low-temperature positive MR is in line with the general idea that the spin ordering enhances localization of carriers, while the destruction of the SDW leads to the delocalization of charge carriers and a decrease in the resistance. Comparison of the results of resistance and magnetoresistance measurements on three samples with different concentrations of strontium (Figs. 4, 8, 9, and 11) suggests that the non-linear effects in conductivity increase with decreasing the concentration of strontium.

Conclusion

In the present paper, the low-temperature conductivity of the AFM $La_{2-x}Sr_xCuO_4$ cuprates with strontium concentration $x \le 0.01$ obtained by solid phase synthesis was studied for the first time.

It was shown that in the temperature range T < 100 K the conductivity mechanism corresponds to 3D variablerange hopping conductivity. Once the AFM order is destroyed, a transition to the metallic conductivity type occurs.

The results of the magnetic and resistive measurements showed that with decreasing the concentration of strontium impurity, the degree of "extrinsic" disorder and the degree of structural disorder increase.

For all samples with the concentration of strontium $x \le 0.01$, nonlinear effects in low-temperature conductivity and current-controlled NDR were found. Nonlinear effects in conductivity were observed to increase with the degree of structural disorder upon decreasing the concentration of strontium. Nonlinear behavior of the U(J,T) dependence is qualitatively consistent with the mechanism of electron overheating and the "thermal model" of energy transfer from the electron to phonon subsystem.

We discovered low-temperature positive magnetoresistance, the magnitude of which depends on the current, temperature, and the degree of structural disorder. It is assumed that the mechanism of positive MR may be linked to the formation of a low-temperature magnetic phase—spin density waves.

Results of the study of lowly doped $La_{2-x}Sr_xCuO_4$ cuprates revealed that the role of internal disorder and local inhomogeneities in the behavior of the conductivity of cuprates is not yet fully understood and further study of the influence of disorder on the properties of HTSC cuprates is required.

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Translated by L. Gardt